

## II – Password-Authenticated Key Exchange

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### Diffie-Hellman Key Exchange

Diffie-Hellman protocol: allows two parties to agree on a common session key:  
In a finite cyclic group  $\mathcal{G}$ , of prime order  $p$ , with a generator  $g$

$$\begin{array}{ccc} x \xleftarrow{\$} \mathbb{Z}_p, X \leftarrow g^x & \xrightarrow{X} & y \xleftarrow{\$} \mathbb{Z}_p, Y \leftarrow g^y \\ K \leftarrow Y^x = g^{xy} & \xleftarrow{Y} & K \leftarrow X^y = g^{xy} \end{array}$$

No authentication provided

#### Authenticated Key Exchange

**Semantic security / Implicit Authentication:**

the session key should be indistinguishable from a random string  
to all except the expected players

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### Authentication Techniques

#### Asymmetric technique

- Assume the existence of a public-key infrastructure
- Each party holds a pair of secret and public keys

#### Symmetric technique

- Users share a random secret key

#### Password-based technique

- Users share a random *low-entropy* secret: **password**

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# Electronic Passport

Since 1998, some passports contain digital information on a chip  
Standards specified by ICAO (International Civil Aviation Organization)



In 2004, security introduced:

- encrypted communication between the chip and the reader
- access control: BAC (Basic Access Control)

The **shared secret** is on the MRZ  
(Machine Readable Zone)

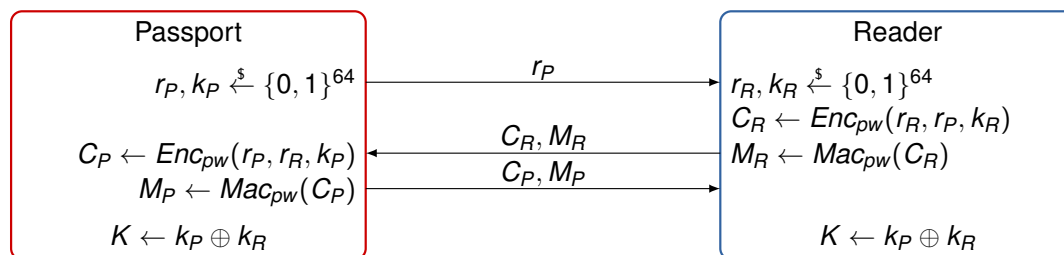
It has low entropy:  
at most 72 bits,  
but actually approx. 40

⇒ low-entropy shared secret: a **password**  $pw$



## BAC: Basic Access Control

The symmetric encryption and MAC keys are deterministically derived from  $pw$



From a pair  $(C_R, M_R)$ , one can make an exhaustive search  
on the password  $pw$  to check the validity of the Mac  $M_R$

After a few eavesdroppings only : **password recovery**

**What can we expect from a low-entropy secret?**

## Off-line Dictionary Attacks

As in the previous scenario, after having

- eavesdropped some (possibly many) transcripts
- interacted (quite a few times) with players

the adversary accumulates enough information  
to take the real password apart from the dictionary

⇒ Efficient password-recovery after **off-line exhaustive search**

For the BAC: quite a few **passive eavesdroppings** are enough to recover the password!

How many **active interactions** could one enforce?

# On-line Dictionary Attacks

## On-line Dictionary Attacks

- The adversary interacts with a player, trying a password
- In case of success: it has guessed the password
- In case of failure: it tries again with another password

## In Practice

- This attack is unavoidable
- If the failures for a target user can be detected the impact can be limited by various techniques
- If the failures cannot be detected (anonymity, no check, ...) the impact can be dramatic

## Outline

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- Intuition
- Find-then-Guess Security
- Examples
- Real-or-Random Security

#### 2 Universal Composability

- Definition
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- Advanced Security Notions
- Examples

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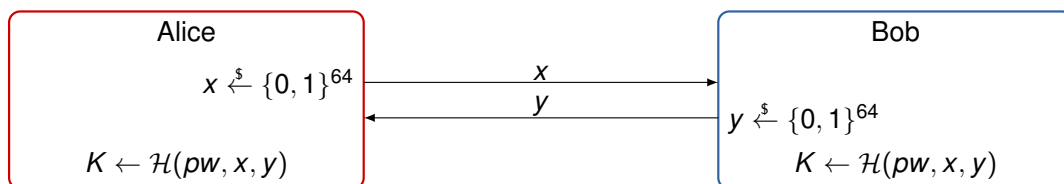
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## First Attempt



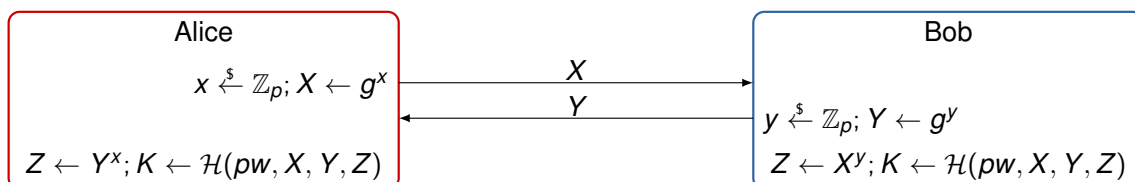
Seems better than BAC: no information leaks about  $K$ , so no leakage about  $pw$  either!

But  $K$  will be later used:  $c = E_K(m)$

any information about  $m$  leaks about  $K$ , and leaks on  $pw$ ...

⇒ The security model has to deal with information leakage about  $K$

## Second Attempt



Passive eavesdropping, even with leakage of  $K$ : secure under **CDH**!

But the adversary can try to impersonate Bob, and know  $Z$ ...

⇒ The security model has to deal with active attacks

## ■ Game-based Security

[Bellare-P.-Rogaway – Eurocrypt '00]

- Find-then-Guess
- Real-or-Random

[Abdalla-Fouque-P. – PKC '05]

## ■ Simulation-based Security

[Boyko-MacKenzie-Patel – Eurocrypt '00]

## ■ Universal Composability

[Canetti-Halevi-Katz-Lindell-MacKenzie – Eurocrypt '05]

Where

- The adversary controls the network: it can create, alter, delete, duplicate messages
- Users can participate in concurrent executions of the protocol

On-line dictionary attack should be the best attack

⇒ No adversary should win with probability greater than  $q_S/N$   
where  $q_S = \# \text{Active Sessions}$  and  $N = \# \text{Dictionary}$

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## Game-based Security

[Bellare-P.-Rogaway – Eurocrypt '00]

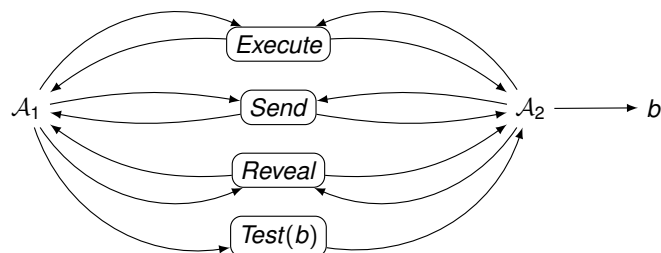
The adversary  $\mathcal{A}$  interacts with oracles:

- $Execute(A^i, B^i)$   
 $\mathcal{A}$  gets the transcript of an execution between  $A$  and  $B$   
⇒ Passive attacks (eavesdropping)
- $Send(U^i, m)$   
 $\mathcal{A}$  sends the message  $m$  to the instance  $U^i$   
⇒ Active attacks against  $U^i$  (active sessions)
- $Reveal(U^i)$   
 $\mathcal{A}$  gets the session key established by  $U^i$  and its partner  
⇒ Leakage of the session key, due to a misuse
- $Test(U^i)$  a random bit  $b$  is chosen
  - If  $b = 0$ ,  $\mathcal{A}$  gets the session key (*i.e.*,  $Reveal(U^i)$ )
  - If  $b = 1$ ,  $\mathcal{A}$  gets a random key

## Security Game: Find-then-Guess

**Secrecy of the key:** output  $b'$ , the guess of the bit  $b$  involved in the Test-query  
Is the obtained key real or random?

**Constraint:** no *Test*-query on a trivially known key  
i.e., key already revealed through the instance or its partner



$$\text{Adv}^{\text{FiG}}(\mathcal{A}) = 2 \times \Pr[b' = b] - 1 \leq \frac{q_S}{N} + \text{negl}()$$

## Freshness and Partnering

### ■ Partners

Two players are **partners** if they share the same **Session ID**  
Where SID should model ideal executions:

- two players with same SID's and same  $pw$ 's conclude with the same session key
- two players with different SID's or different  $pw$ 's conclude with independent keys

### ■ Freshness

A key or a player is **fresh** if none of the key/player or the partner's key/player has been revealed/tested

Only **fresh** keys/players can be revealed/tested

## Security Notions: Forward Secrecy

### ■ Semantic Security

The **Find-then-Guess** game models the **secrecy** of the key  
 $\implies$  the session key is unknown to the other players

- What about this secrecy after the corruption of a player?
- What about the knowledge of the two players?

### ■ Forward Secrecy

- An additional oracle:  $\text{Corrupt}(U)$  provides the password  $pw$  of the player  $U$  to the adversary
- A new constraint: For any  $\text{Test}(U^i)$ , player  $U$  was not corrupted when  $U^i$  was involved in its session

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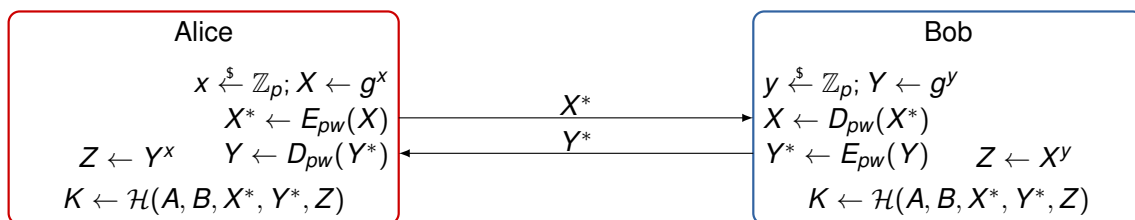
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## Encrypted Key Exchange

[Bellare-Meritt – S&P '92]



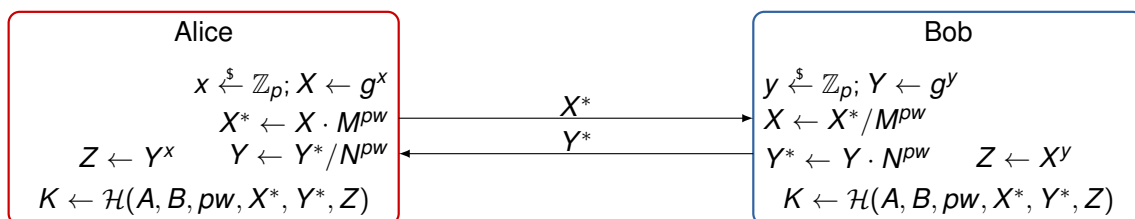
Semantically Secure with Forward Secrecy if

- $(E, D)$  is an Ideal Cipher onto  $\mathbb{G} = \langle g \rangle$
- $\mathcal{H}$  is a Random Oracle

[Bellare-P.-Rogaway – Eurocrypt '00]

## Simple PAKE

[Abdalla-P. – CT-RSA '05]



Semantically Secure if

- **CDH**( $M, N$ ) hard to break
- $\mathcal{H}$  is a Random Oracle

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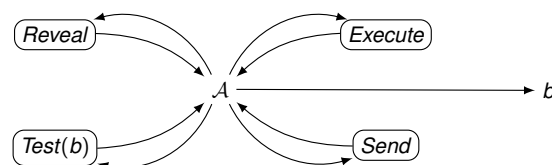
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## Security Game: Real-or-Random

[Abdalla-Fouque-P. – PKC '05]

**Secrecy/independence** of all the keys: many *Test*-queries with the same bit  $b$

- If no key defined by the protocol yet: output  $\perp$
- If dishonest/corrupted partner: output the real key
- If player/partner already tested (not fresh): output the same key
- If  $b = 0$ : output the real key
- If  $b = 1$ : output a random key



$$Adv^{RoR}(\mathcal{A}) = 2 \times \Pr[b' = b] - 1$$

## Security Game: Real-or-Random

### Semantic Security (Encryption)

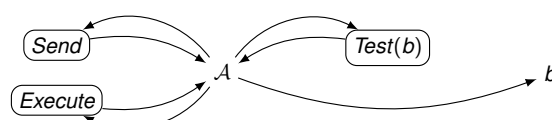
[Bellare-Desai-Jokipii-Rogaway – FOCS '97]

Find-then-Guess and Real-or-Random are polynomially equivalent

$$Adv^{RoR}(t, q_T) \leq q_T \times Adv^{FtG}(t)$$

where  $q_T$  is the number of Test-queries

- For Password-based Authenticated Key Exchange:  
 $Adv^{FtG}(t) \leq \frac{q_S}{N} \not\Rightarrow Adv^{RoR}(t, q_T) \leq \frac{q_S}{N} \Rightarrow$  **Stronger notion**
- No need of Reveal-queries  $\Rightarrow$  **Simpler security notion** [Abdalla-Fouque-P – PKC '05]





# Game-based Security: Limitations

- Proven bounds:  $O(q_S)/N$ , but almost never  $q_S/N$

⇒ hard to get optimal bound!

This means: a few passwords can be excluded by each active attack

But  $q_S$  is sometimes the **number of Send-queries**

which is more than the **number of Active Sessions**

- Passwords chosen from pre-determined, known distributions
- Different passwords are assumed to be independent
- No security guarantees under arbitrary compositions

⇒ **Universal Composability** more appropriate

[Canetti – FOCS '01]

[Canetti-Halevi-Katz-Lindell-MacKenzie – Eurocrypt '05]

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# Definition

## Real Protocol

The real protocol  $\mathcal{P}$  is run by players  $P_1, \dots, P_n$ ,  
with their own private inputs  $x_1, \dots, x_n$ .  
After interactions, they get outputs  $y_1, \dots, y_n$

## Ideal Functionality

An ideal function  $\mathcal{F}$  is defined:

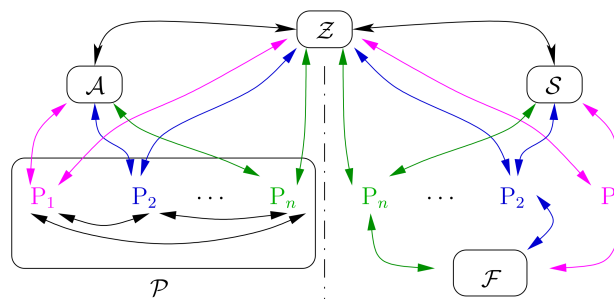
- it takes as input  $x_1, \dots, x_n$ ,  
the private information of each player,
- and outputs  $y_1, \dots, y_n$ , given privately to each player

The players get their results, without interacting:  
this is a “by definition” secure primitive

# Simulator

$\mathcal{P}$  **emulates**  $\mathcal{F}$  if, for any environment  $\mathcal{Z}$ , for any adversary  $\mathcal{A}$ ,  
there exists a simulator  $\mathcal{S}$  so that, the view of  $\mathcal{Z}$  is the same for

- $\mathcal{A}$  attacking the real protocol  $\mathcal{P}$
- $\mathcal{S}$  attacking the ideal functionality  $\mathcal{F}$



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## Queries

- `NewSession` = a player joins the system with a password
- `TestPwd` =  $\mathcal{A}$  attempts to guess a password (**one** per session)  
The adversary learns whether the guess was correct or not
- `NewKey` =  $\mathcal{A}$  asks for the session key to be computed and delivered to the player

## Corruption-Query

- $\mathcal{A}$  gets the long-term secrets ( $pw$ ) and the internal state
- $\mathcal{A}$  takes the entire control on the player and plays on its behalf

Corruptions can occur **before the execution**: Static Corruptions  
Corruptions can occur **at any moment**: Adaptive Corruptions

## Session Key

- No corrupted players, same passwords  
⇒ same key, randomly chosen
- No corrupted players, different passwords  
⇒ independent keys, randomly chosen
- A corrupted player  
⇒ key chosen by the adversary
- Correct password guess (`TestPwd`-query)  
⇒ key chosen by the adversary
- Incorrect password guess (`TestPwd`-query)  
⇒ independent keys, randomly chosen

## Properties

- The `TestPwd`-query models the on-line dictionary attacks
- The `Corruption`-query includes forward-secrecy

## Advantages wrt Game-based Security

- No assumption on the distribution of passwords (chosen by the environment)
- Passwords can be related (it models mistyping)
- Security under arbitrary compositions ⇒ **secure channels**

# Game-based Security vs. Universal Composability

## Game-based Security

In the reduction, the simulator has to emulate the protocol execution

**only** up to an evidence the adversary has won ( $pw \Rightarrow \text{not negl.}$ )

In the global system, the simulation fails when the adversary breaks one sub-protocol whereas other parts could provide protection ( $pw \Rightarrow \text{weak proof!}$ )

## UC Security

Simulation handles compositions, but proofs are more complex:

the simulator must have an indistinguishable behavior, even when the adversary wins!

In the case of **password-based cryptography**:

the adversary can win with non-negligible probability!

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## Properties of the $\text{NewKey-Query}$

### Session Key: $\text{NewKey-Query}$

...

- A corrupted player  $\Rightarrow$  key chosen by the adversary
- Correct password guess  $\Rightarrow$  key chosen by the adversary

...

The  $\text{NewKey-query}$  models possible **Key Distribution**:

$\Rightarrow$  the session key can be controlled by one of the players

The contributiveness property models **Key Agreement** [Adalla-Catalano-Chevalier-P. – CT-RSA '09]

$\Rightarrow$  no player can decide on the key

# Properties of the TestPwD-Query

## Dictionary Attack: TestPwD-Query

- Correct password guess  $\implies$  key chosen by the adversary
- Incorrect password guess  $\implies$  random key

And adversary **informed** of correct/incorrect guess

The TestPwD-query models **Explicit Authentication**:

$\implies$  the players are informed of success/failure

Implicit-Only PAKE models **Implicit Authentication** [Dupont-Hesse-P.-Reyzin-Yakoubov – Eurocrypt '18]

$\implies$  they keys have to be used to test success/failure

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## UC-Secure PAKE

With a random oracle and an ideal cipher: EKE

[Abdalla-Catalano-Chevalier-P. – CT-RSA '08]

$\implies$  First efficient scheme secure against **Adaptive Corruptions**

In the standard model, based on GL (abstraction of KOY)

$\implies$  BPR-security using SPHF

[Gennaro-Lindell – Eurocrypt '03]

- with SS-ZK  $\implies$  **Static corruptions**

[Canetti-Halevi-Katz-Lindell-MacKenzie – Eurocrypt '05]

- with an *equivocal/extractable commitment*

$\implies$  **Adaptive corruptions**

[Abdalla-Chevalier-P. – Crypto '09]

- with KV-SPHF and SS-NIZK  $\implies$  **One-round only**

[Katz-Vaikuntanathan – TCC '11]

- with *Explainable SPHF*

$\implies$  Adaptive corruptions **without erasures**

[Abdalla-Benhamouda-P. – PKC '17]

assuming a CRS (proven impossible in the plain model)

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# Conclusion

EKE is a secure PAKE in the ROM+ICM:

- BPR secure
- UC secure
- Withstands **adaptive corruptions**
- Provides **forward-secrecy**
- Can guarantee **Explicit** or **Implicit-Only** authentication

All the constructions in the standard model exploit SPHF:

- based on the **KOY protocol**
- extend the **GL protocol**

[Katz-Ostrovsky-Yung – Crypto '01]

[Gennaro-Lindell – Eurocrypt '03]

Let us see SPHF-based PAKE Protocols